

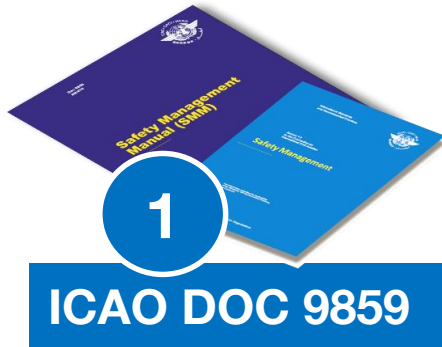


# Landing Trajectory and Touchdown Point Reconstruction

EOFDM Conference 2016

Joachim Siegel, Lukas Höhndorf

# General Concept



- Airlines are required to implement a safety management system (SMS)
- SMS requires operators also to define their own **Acceptable Level of Safety (ALoS)**.

- **Europe** aims at less than one accident per ten million flights (i.e. **accident probability of  $10^{-7}$  per flight**).



Flightpath 2050

**Central question: What is the current safety level of my airline?**

# General Concept



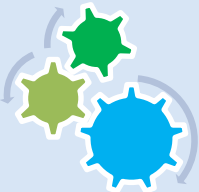
$$P_{\text{Accident}} = \frac{\text{Number of accidents}}{\text{Number of flights}}$$

Classical statistical approach



$$P_{\text{Accident}} = \frac{0}{400\,000} = 0$$

Runway overrun example



## Developed Predictive Analysis

Making **quantitative statements** about the future state based on **previous experience and knowledge**.

Compare the presentations of Ludwig Drees and Javensius Sembiring (TUM-FSD) at the EOFDM Conference 2014



# Problem Statement and Objective

- Recorded data always contain errors and uncertainties!
- Example: Bad quality of position data (if you consider them solely) can make a thorough touchdown analysis impossible
- Often, the sampling rate of position data is low

Compare the presentation “Landing trajectory computation” of Géraud de Rivals (Airbus) at EOFDM Conference 2014

## Raw data GPS trajectory

Source: Google Earth

### 1.) Improve trajectory

- Increase sampling rate
- Reduce influence of data recording errors
- Physically more meaningful trajectory

### 2.) Correct lateral offset

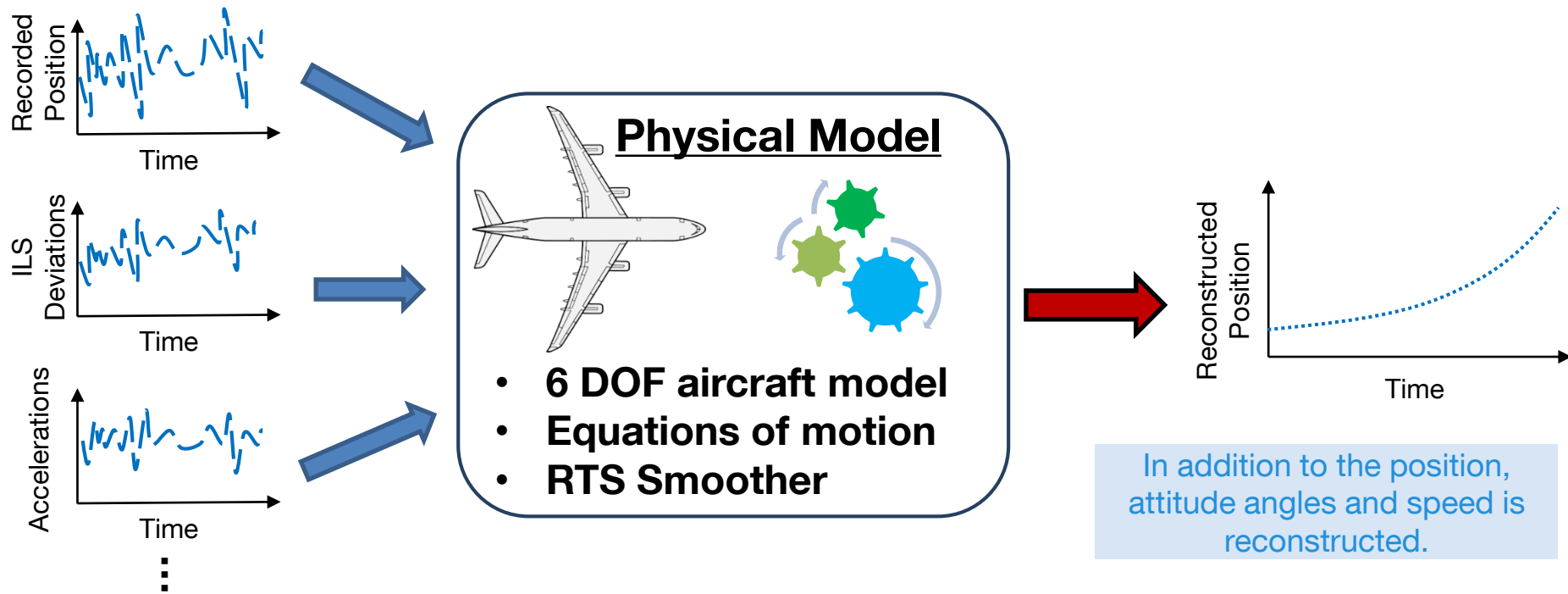
### 3.) Correct longitudinal offset

Source: Google Earth

## Reconstructed trajectory

# Concept

## Mathematical Method: State Estimation using Rauch-Tung-Striebel (RTS) Smoother

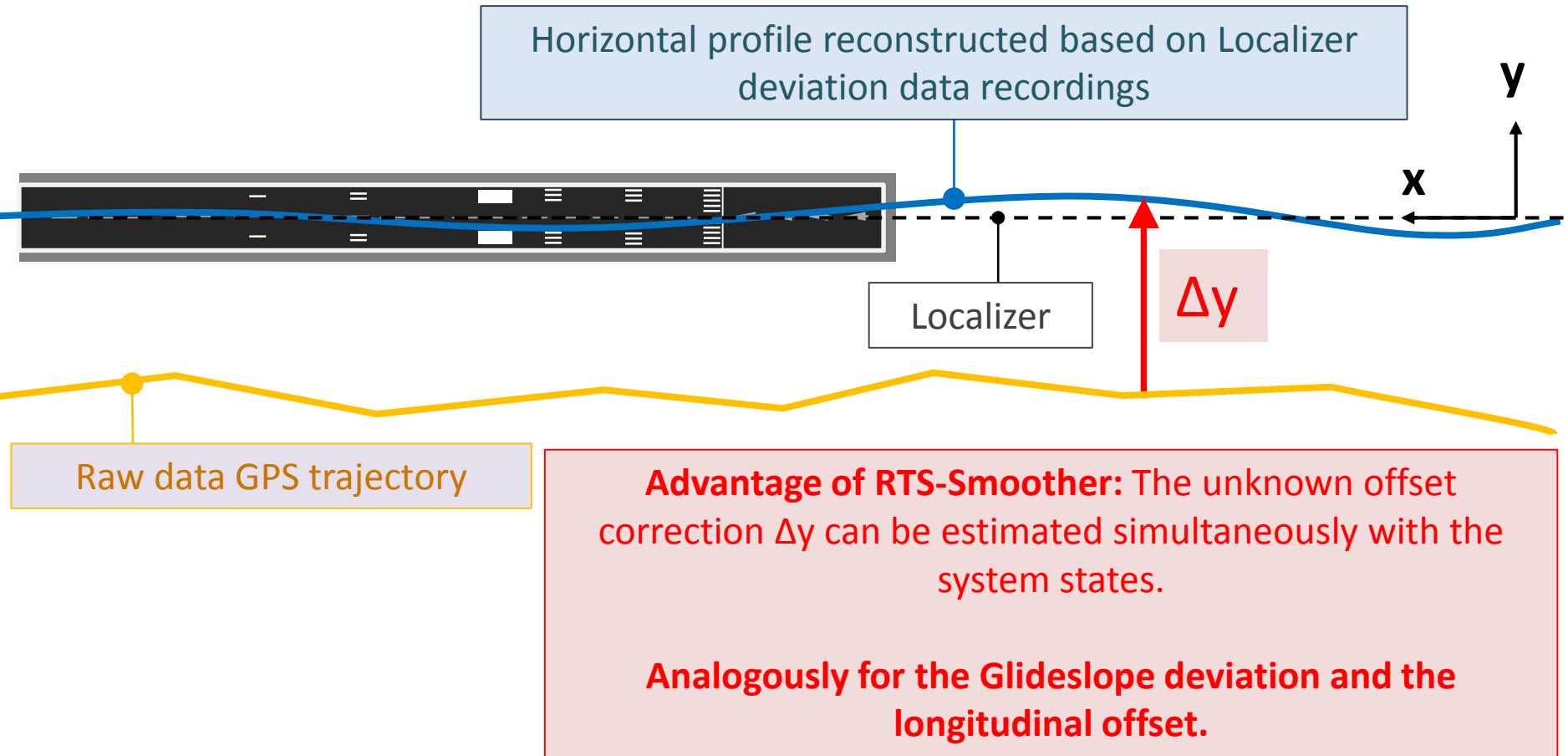


The RTS Smoother is an advanced Kalman Filter that is already used in modern aircraft for navigation purposes.

Advantage of (offline) FDM compared to online application in the cockpit: Past AND FUTURE data recordings can be taken into account!

# Correct Lateral Offset

**Mathematical Method: Estimate offset  $\Delta y$  by use of Localizer deviation data recordings**





# RTS Smoother Output

Source: Google Earth

Trajectory after application of RTS Smoother | 8 Hz

Raw data GPS trajectory | 0.5 Hz

Remaining offset to taxiway centerline: approx. 50 m

## 1.) Improve trajectory

- Increase sampling rate
- Reduce influence of data recording errors
- Physically more meaningful trajectory



## 2.) Correct lateral offset



## 3.) Correct longitudinal offset



Why?

# RTS Smoother Output

## 3.) Correct longitudinal offset



**Why is the achieved longitudinal offset correction worse than the lateral?**

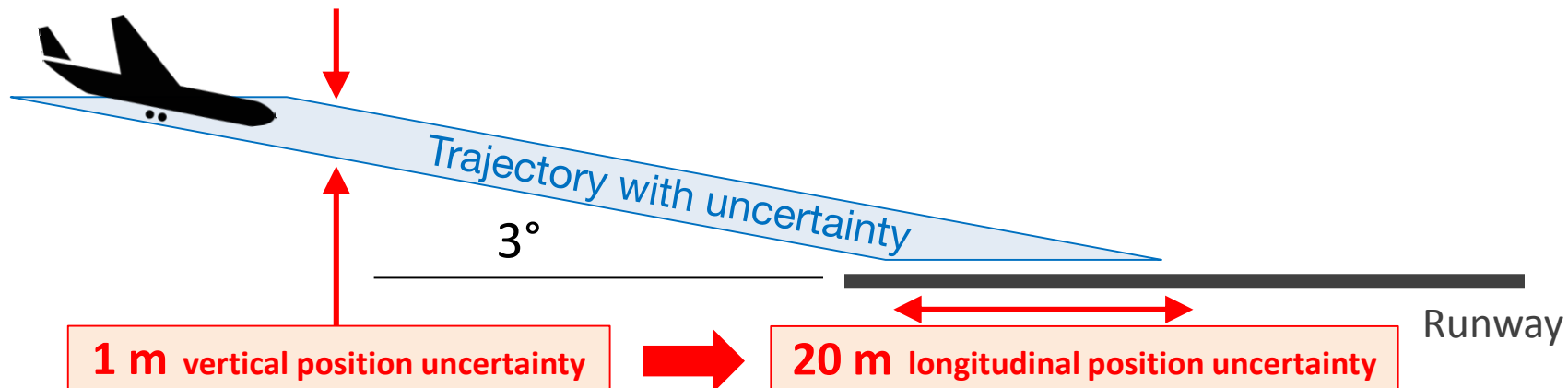
### 1) Precise reconstruction of altitude above threshold is difficult

- Combination of Radio Altitude, WGS 84 Altitude and Barometric Altitude
- Many corrections have to be applied

### 2) Imperfect knowledge of glide path intersection point

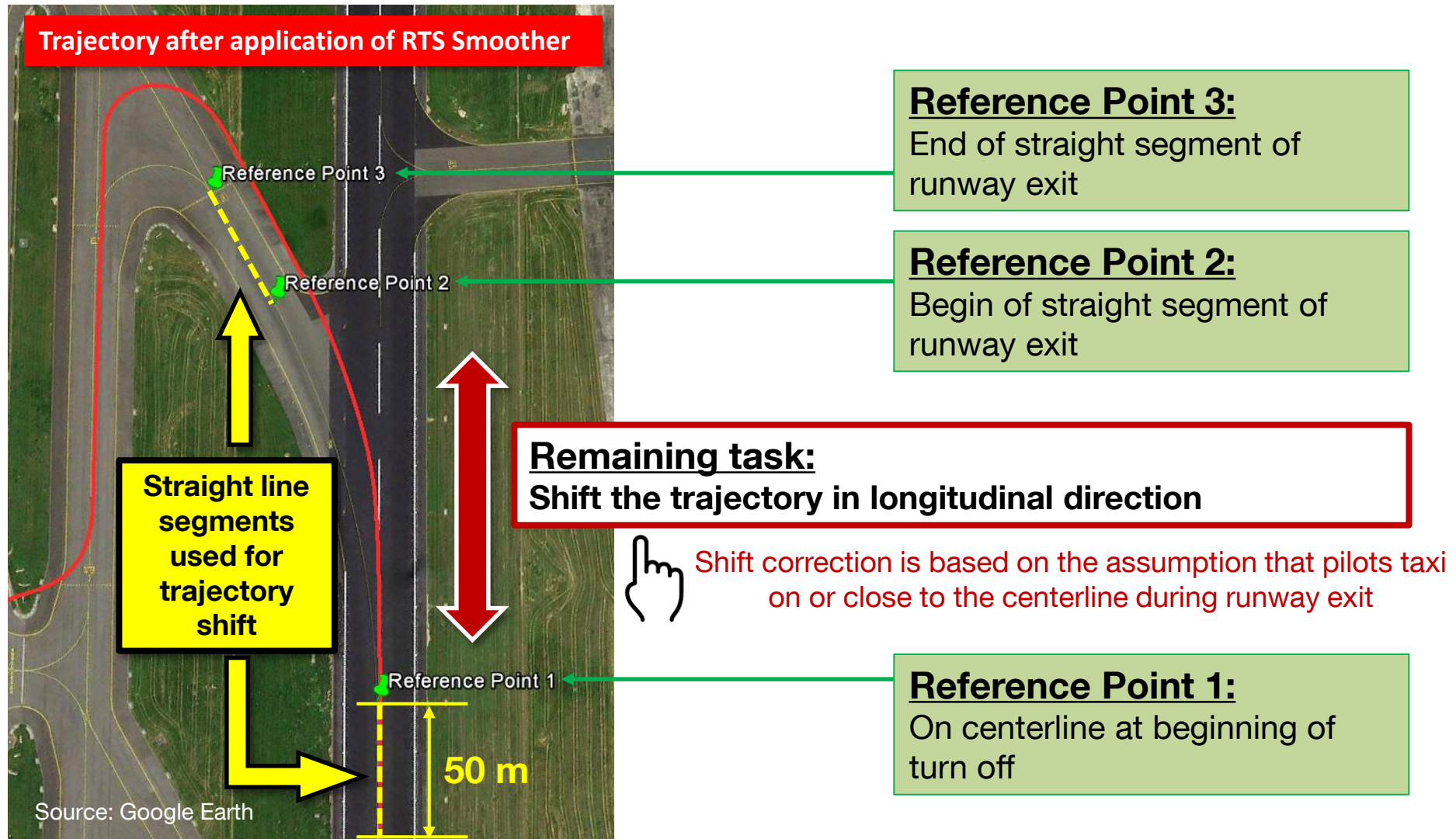
- Glide path antenna position is used instead

### 3) Strong error amplification due to small Glideslope angle



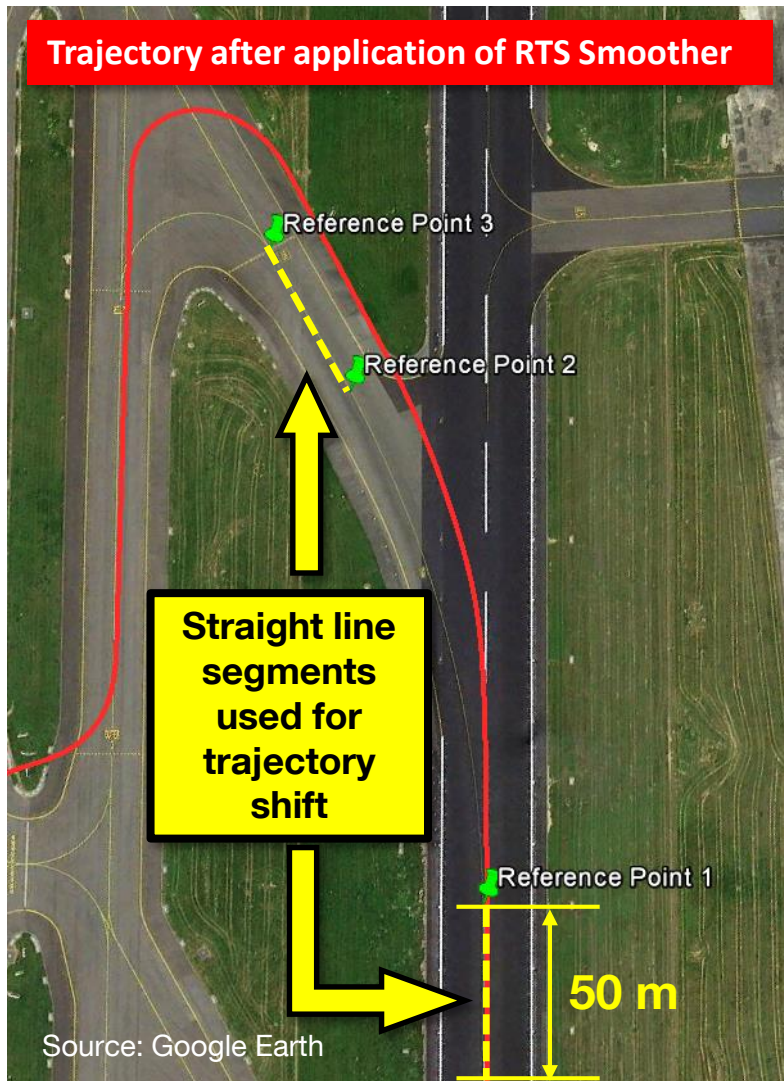


# Longitudinal Shift Correction Based on Runway Exit

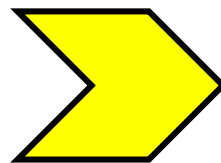


# Longitudinal Shift Correction Based on Runway Exit

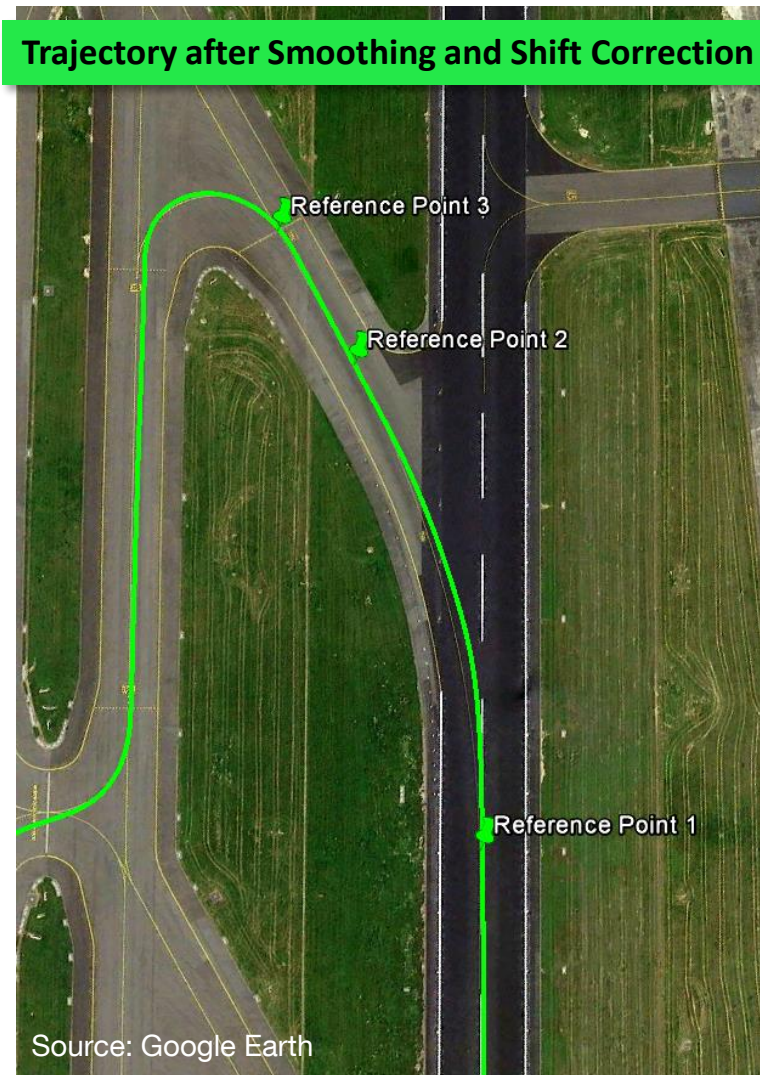
**Trajectory after application of RTS Smoother**



**Automatic  
runway exit  
identification  
and shift  
correction**



**Trajectory after Smoothing and Shift Correction**





# RTS Smoother Output

Source: Google Earth

Trajectory after Smoothing and Shift Correction | 8 Hz

Raw data GPS trajectory | 0.5 Hz

## 1.) Improve trajectory

- Increase sampling rate
- Reduce influence of data recording errors
- Physically more meaningful trajectory



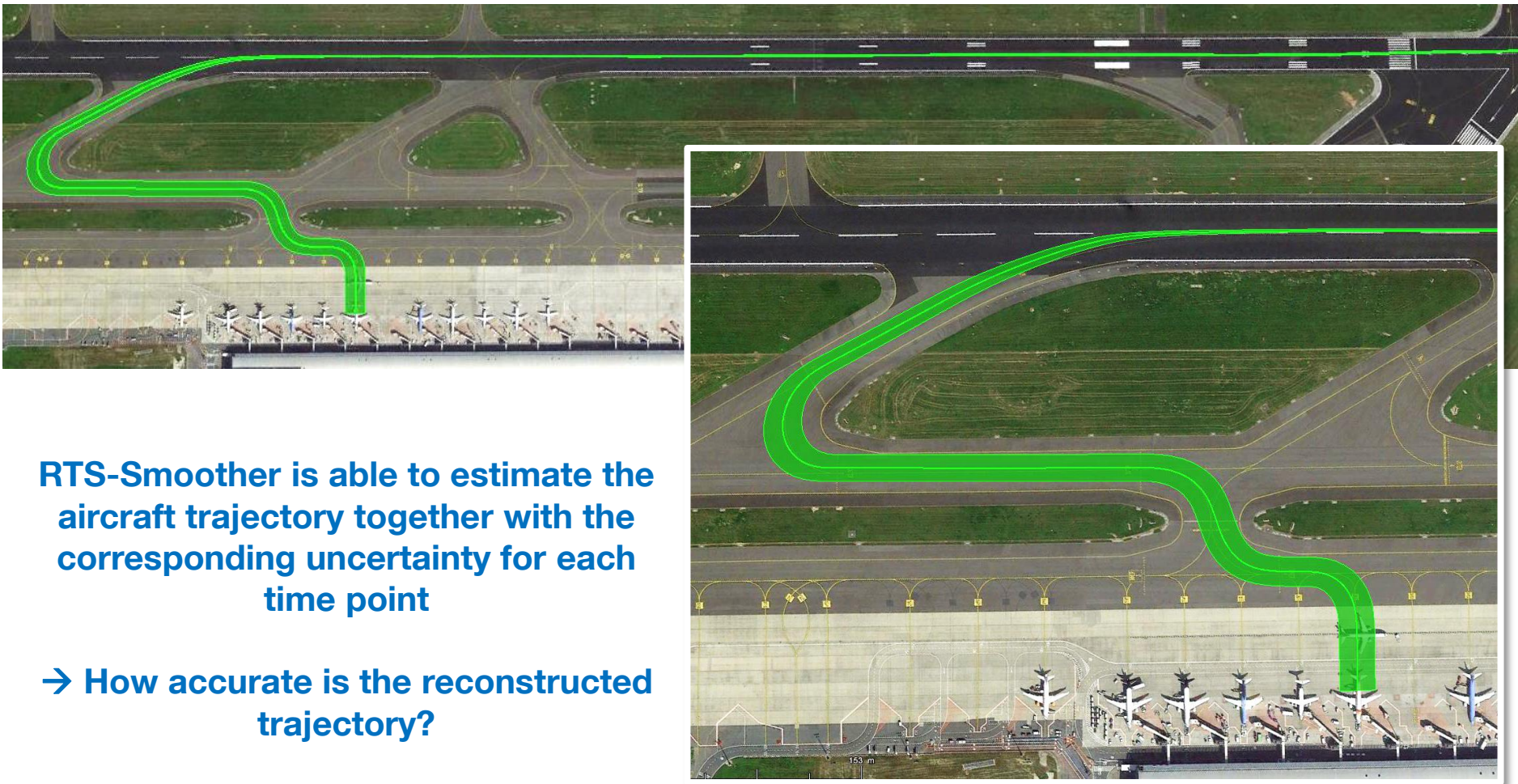
## 2.) Correct lateral offset



## 3.) Correct longitudinal offset



# Final Result of Trajectory Reconstruction

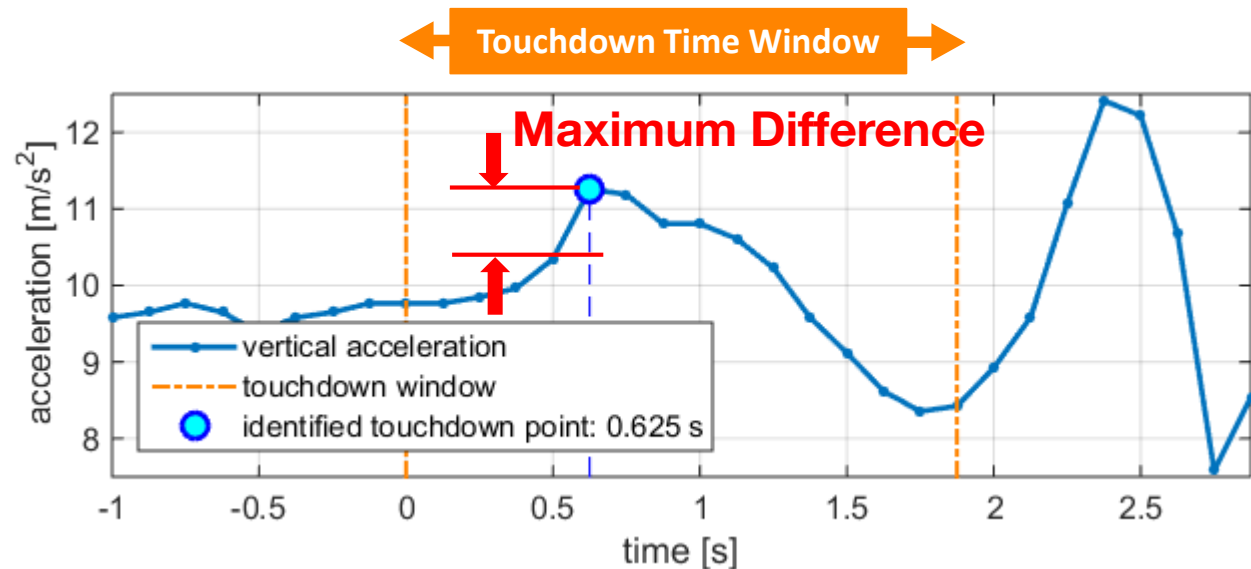




# Common Touchdown Point Detection Methods

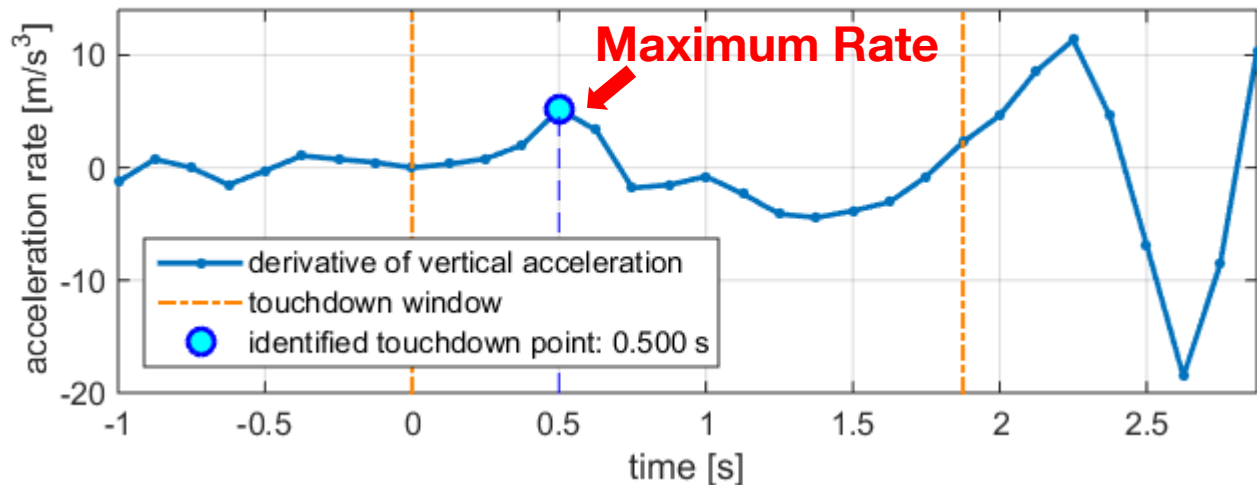
## Method 1 - Maximum Difference Strategy

Seek highest difference in vertical acceleration



## Method 2 - Maximum Rate Strategy

Seek maximum in derivative of vertical acceleration



# Model Based Touchdown Point Detection

Angle of Attack

Angle of Attack Rate

Pitch Rate

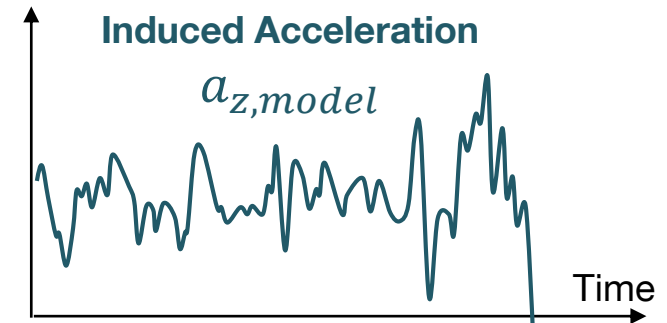
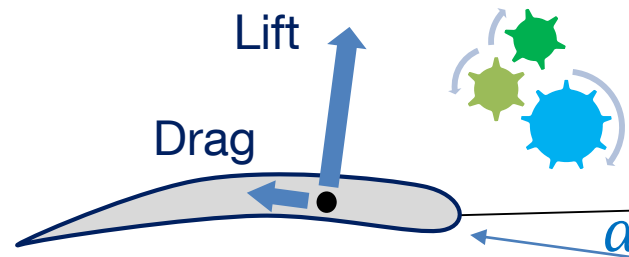
Elevator Deflection

Stabilizer Position

Spoiler Deflection

Aerodynamic Model for  
Vertical Acceleration

$a_{z,model}$



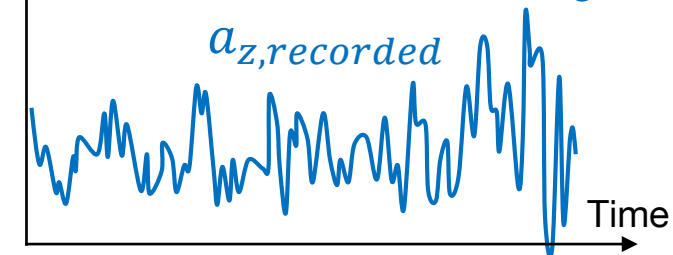
**Model DOES NOT include  
acceleration caused by  
ground reaction force**

Direct Acceleration  
Recording  $a_{z,recorded}$

$a_{z,recorded}$



Direct Acceleration Recording

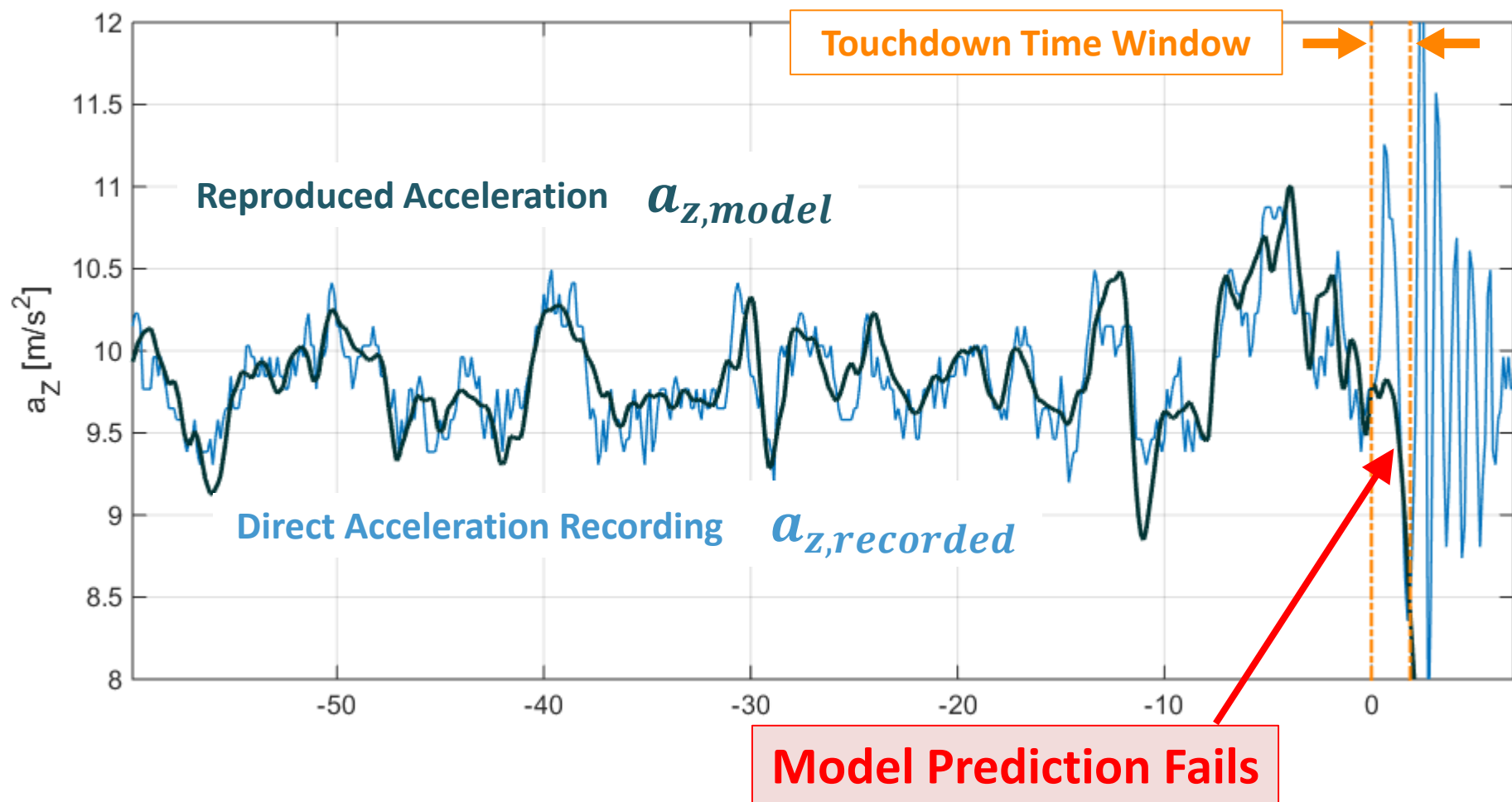


**Direct recording DOES  
include acceleration caused  
by ground reaction force**

Vertical Acceleration



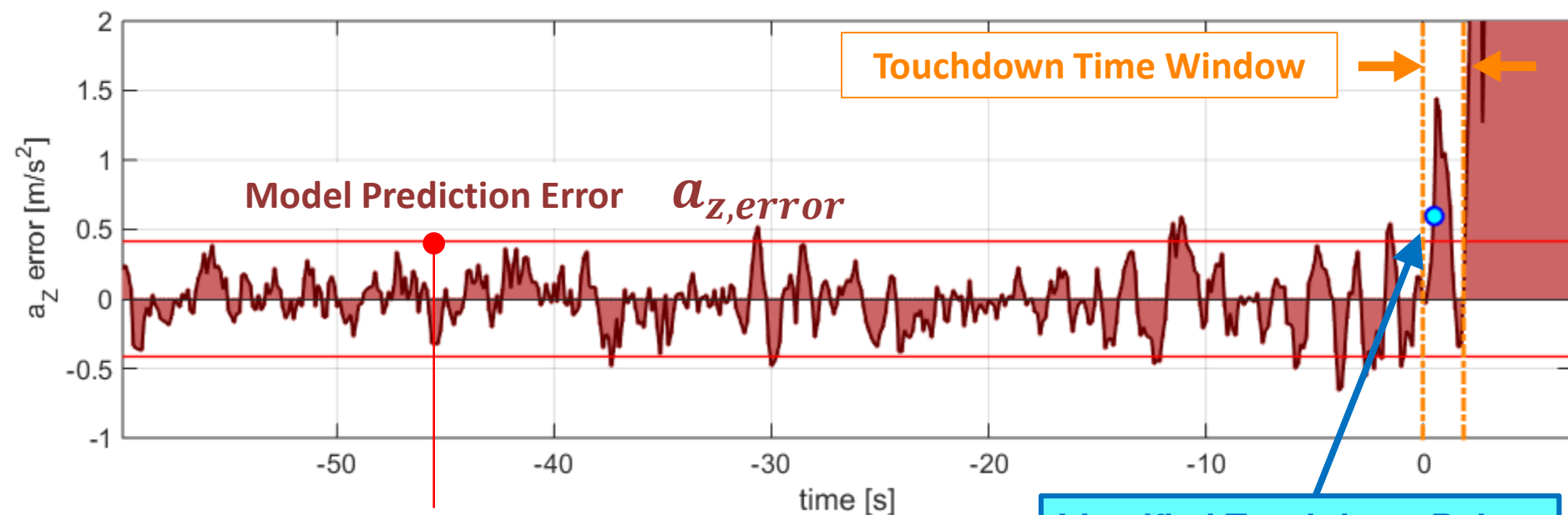
# Model Based Touchdown Point Detection



# Model Based Touchdown Point Detection

**Metric to detect the model failure: Model Prediction Error**

$$a_{z,error} = a_{z,recorded} - a_{z,model}$$



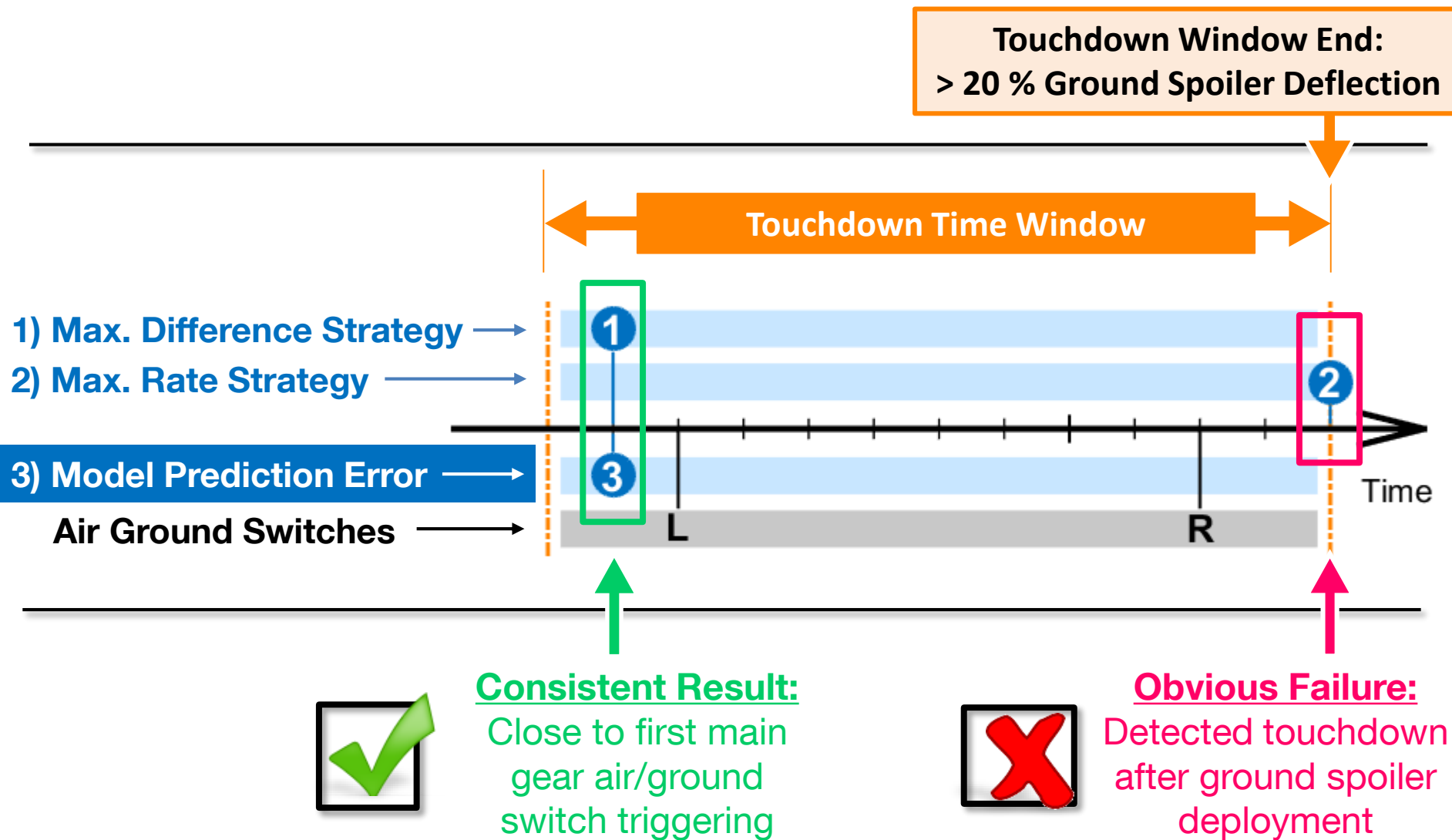
**Boundary of 2 Standard Deviations**

Based on the model prediction errors before the touchdown time window

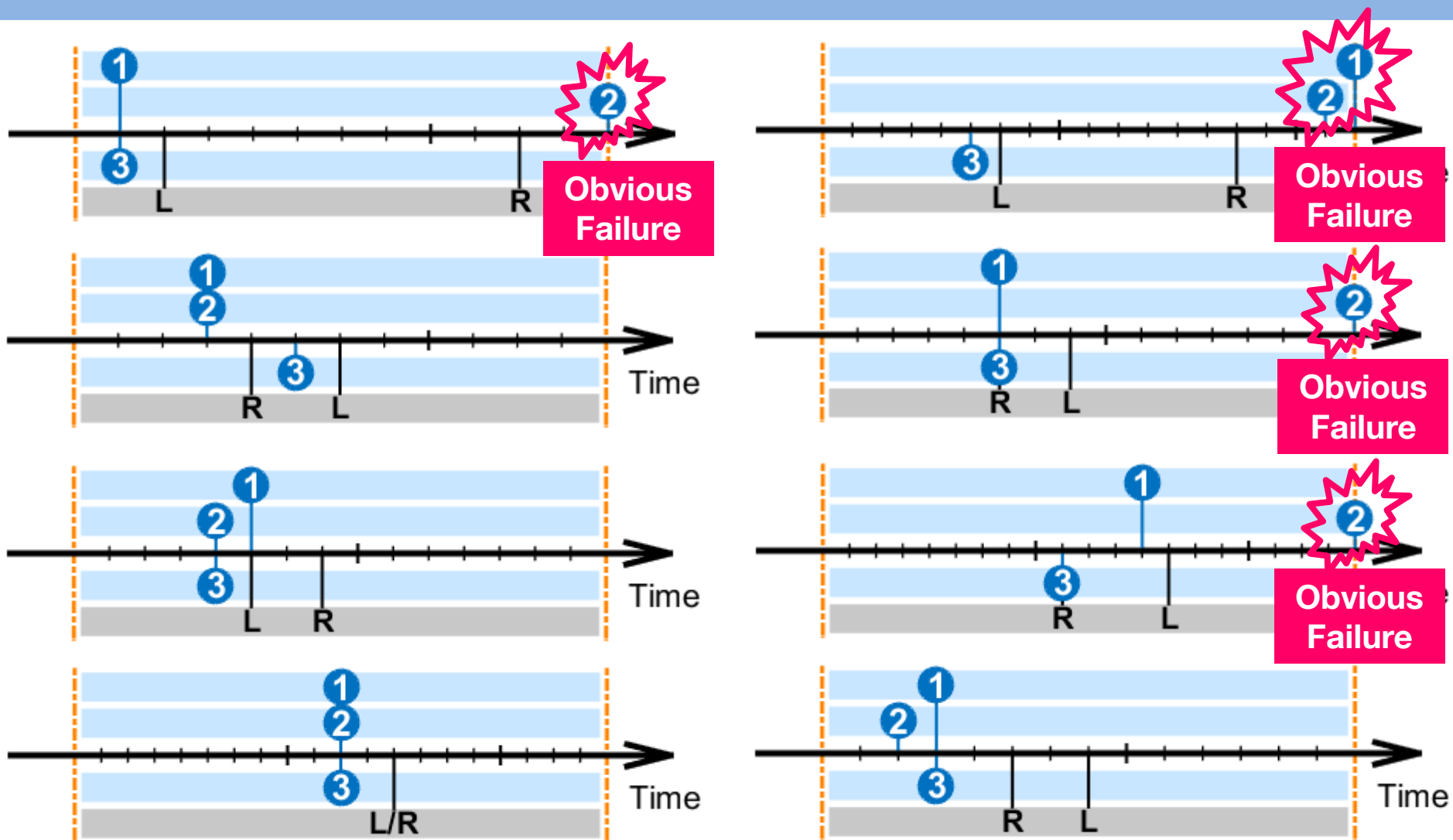
**Identified Touchdown Point**

First time point with model prediction error at least 10 % above 2 sigma boundary

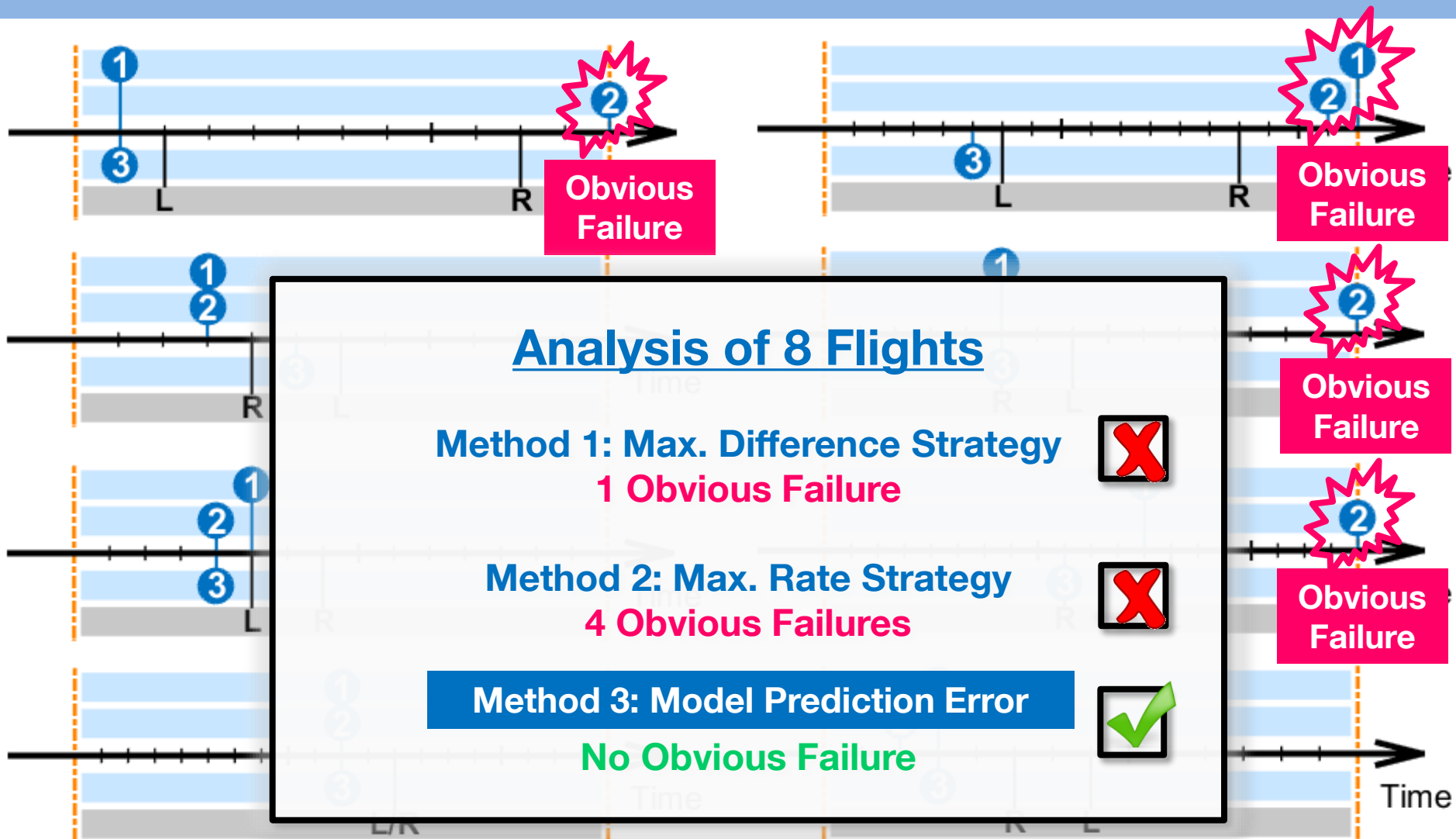
# Results of the Touchdown Point Detection



# Results of the Touchdown Point Detection



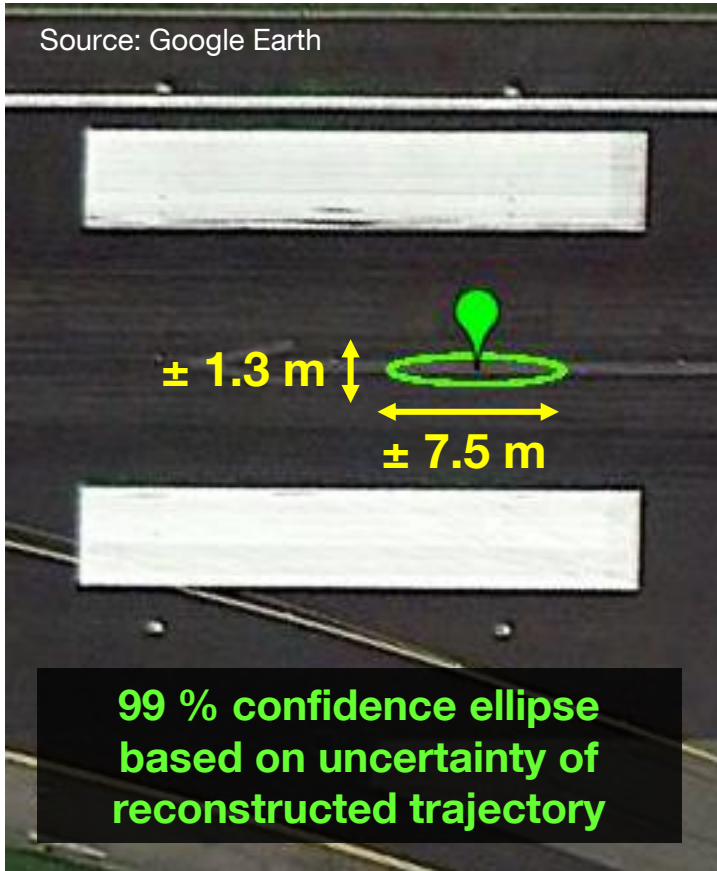
# Results of the Touchdown Point Detection



# Preliminary Accuracy Assessment

## Touchdown Point Result:

Source: Google Earth



## Longitudinal Error (99 % confidence)

- |                                      |                      |
|--------------------------------------|----------------------|
| a) Uncertainty of trajectory         | <b>± 7.5 m</b>       |
| b) Taxiway shift correction error *  | <b>± 5 to ± 10 m</b> |
| c) Touchdown time point detection ** | <b>± 18 m</b>        |

---

Combined Error ( $\sqrt{a^2 + b^2 + c^2}$ ) **± 20 to ± 22 m**

## Lateral Error (99 % confidence)

- |                                   |                |
|-----------------------------------|----------------|
| a) Uncertainty of trajectory      | <b>± 1.3 m</b> |
| b) Taxiway shift correction error | <b>n.a.</b>    |
| c) Touchdown time point detection | <b>± 0.5 m</b> |

---

Combined Error ( $\sqrt{a^2 + c^2}$ ) **± 1.6 m**

\* Depending on taxiway angle / based on the assumption, that pilots taxi within ± 5 m of taxiway centerline 99 % of time

\*\* Based on the assumption, that in 99 % of all cases the correct touchdown time point is identified within ± 2 samples



# Future Plans

- Application of the algorithm to a variety of flights (especially in safety critical scenarios such as Florence airport)
- Verification and calibration of the algorithm (e.g. based on aircraft detection in video data or flight test data)
- Evaluate possibilities for integrating the algorithm into existing FDM software



# Summary



## Advantages of a Precise Landing Trajectory and Touchdown Point

Required First Step for Safety Investigations like Predictive Analysis

Enable Sophisticated Analysis of Touchdown Point Distributions

**Reconstructed Trajectory and Touchdown**

Accurate Landing Trajectory can be Used for Visualization and Debriefing

Besides Position, High Quality Reconstruction of Further States (e.g. Speed or Attitude) is Provided



## **Institute of Flight System Dynamics**

Technische Universität München

Boltzmannstraße 15

D-85748 Garching bei München

Deutschland / Germany

Phone: +49 89 289-16080

Fax: +49 89 289-16058

**Joachim Siegel**, joachim.siegel@mytum.de

**Lukas Höndorf**, lukas.hoehndorf@tum.de

**Ludwig Drees**, ludwig.drees@tum.de

**Javensius Sembiring**, javensius.sembiring@tum.de

**Chong Wang**, chong.wang@tum.de

**Phillip Koppitz**, phillip.koppitz@tum.de

**Florian Holzapfel**, florian.holzapfel@tum.de

**In cooperation with Brussels Airlines**

Wilfried van Laer, Simon Kerkhofs



# Thank you for your attention