



**airBaltic**

# Comparing Fuel Flow using a Cluster Method

EOFDM Conference 2016

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# Motivation

Use Shark Skin Effect with Ripplet Structure



Expected drag reduction:  $\approx 1\%$



Measurable effect in normal Operation?



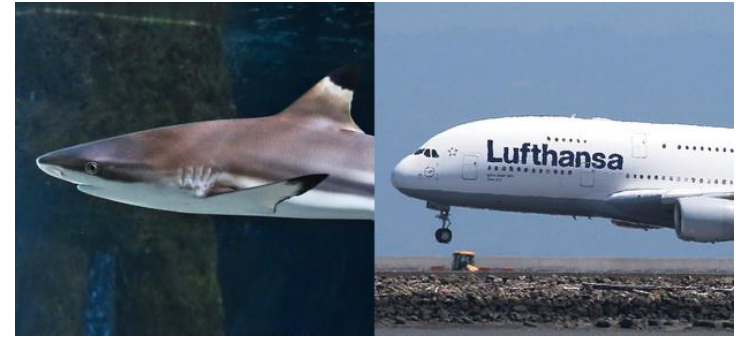
Idea: Cluster fuel flow data based on influencing factors



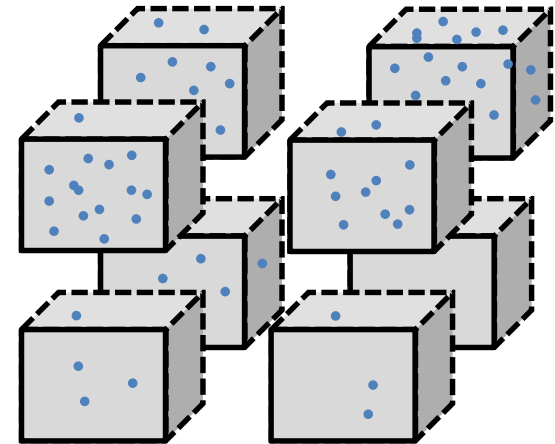
Fuel flow distributions at operating points / areas



Compare data sets at operating points

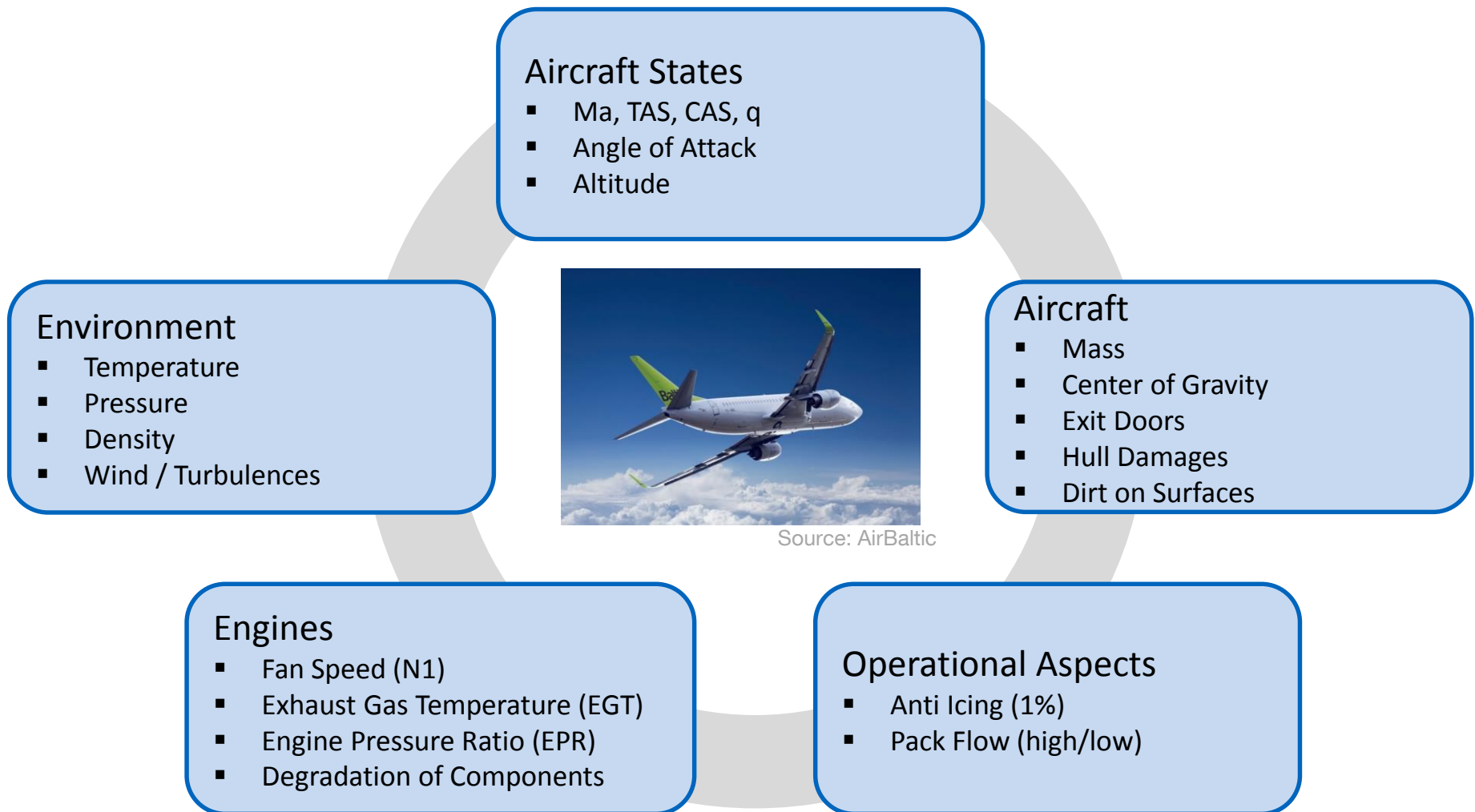


Alexander Klein/AFP/Getty Images, Justin Sullivan/ Getty Images



Application possibilities: fuel flow over time, measure effects of constructive aerodynamic changes, compare fuel flow of a fleet

# Potential Influencing Factors of Fuel Flow



# Concept of Clustering – General Idea

Assumption: fuel flow is function of influencing factors  

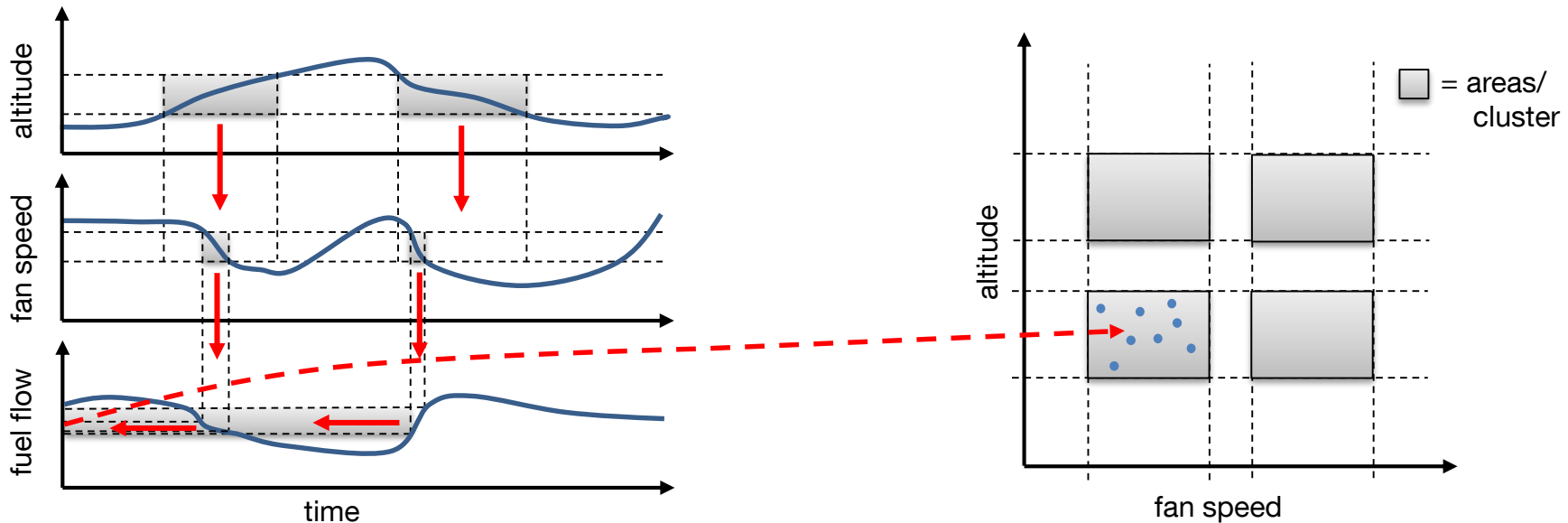
$$\text{fuel flow} = f(N1, Ma, h, m, \dots)$$

Perfect comparability:  
 (if function were known)

Evaluating the function at specific points  
 → Single values of influencing factors

Clustering:  
 (function not known)

Retract measured fuel flow data in different areas  
 → Value intervals of influencing factors



Extendable to any number of influencing factors

# Concept of Clustering – Single Cluster Analysis

Only „full clusters“ are analyzed

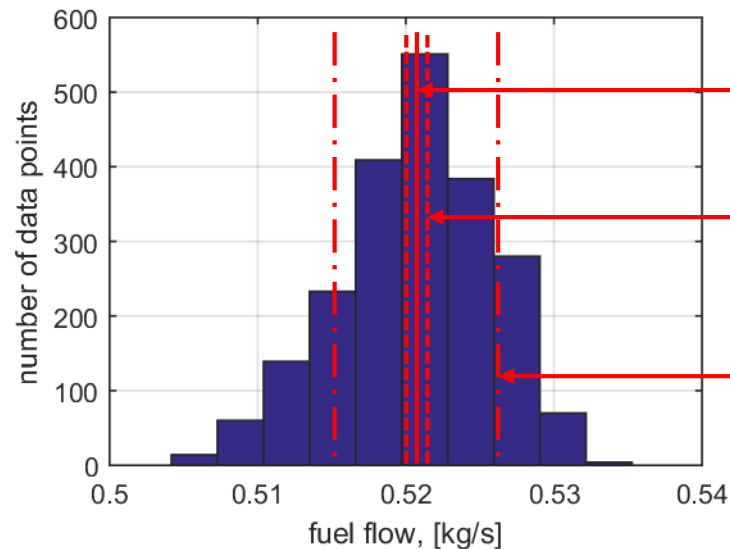
- Minimum number of data points within cluster for statistical confidence



Analysis figures per full cluster:

number of  
data points

number of  
contributing  
flights



mean value

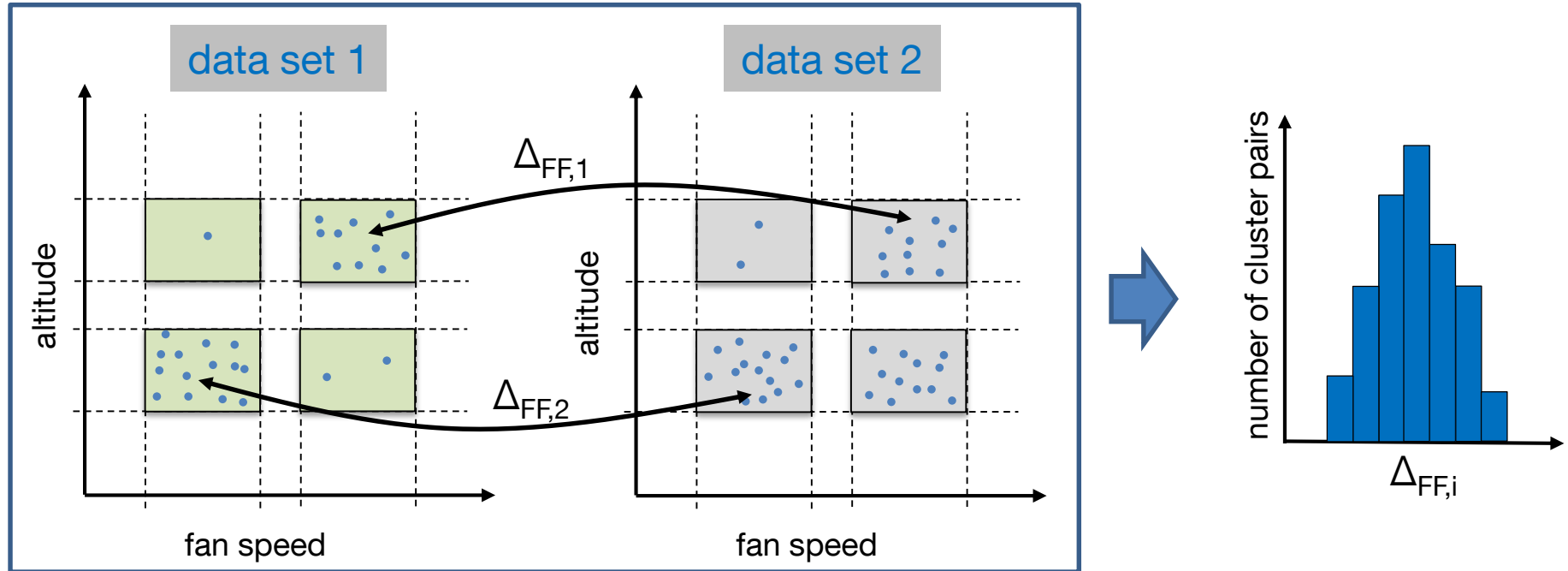
confidence  
interval

standard  
deviation

# Concept of Clustering – Comparing Data Sets

Compare pairs of full clusters of two different data sets

- Calculate difference of mean values of both full clusters ( $\Delta_{FF,i}$ )



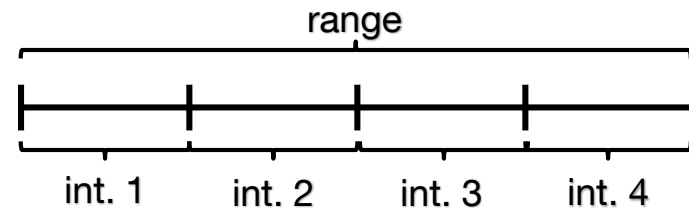
Comparison of multiple data sets via: Mean values of  $\Delta_{FF}$ -distributions of each pairwise combination of data sets

# Analysis – Basic Information

Influencing Factor	Unit	Resolution	Range	Number of Intervals	Width of Intervals
Pressure Altitude	[m]	0.3	FL360 ± 25m	1	50
Fan Speed	[-]	0.001	0.82 - 0.9	8	0.01
Mach Number	[-]	0.002	0.72 - 0.76	4	0.01
Temperature	[K]	0.025	230 - 258	4	7

Four influencing factors divided into equally spaced intervals

- $1 \times 8 \times 4 \times 4 = 128$  clusters per analysis



100 Flights of one aircraft (B737–500)

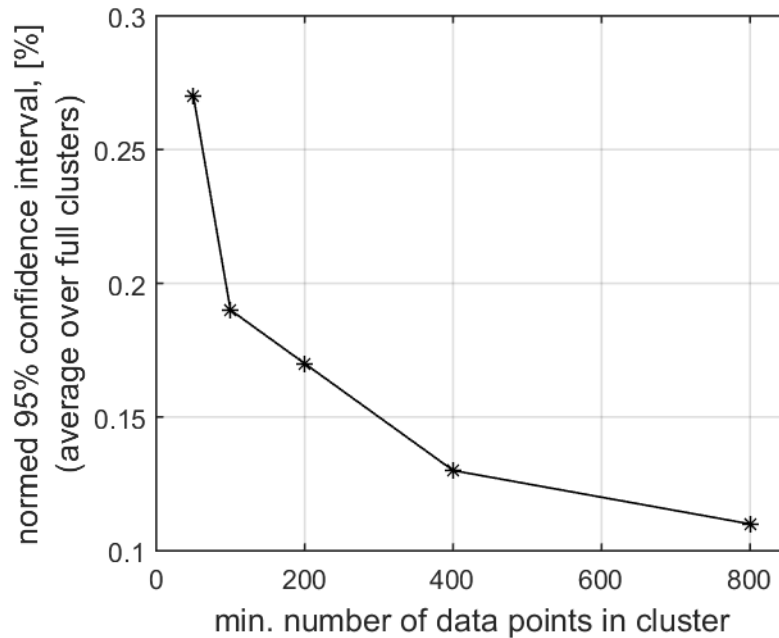
- Mainly short cruise phases
- Flights recorded between January 2013 and July 2014
- Lowest sampling rate defines data points (1 Hz)

Note:

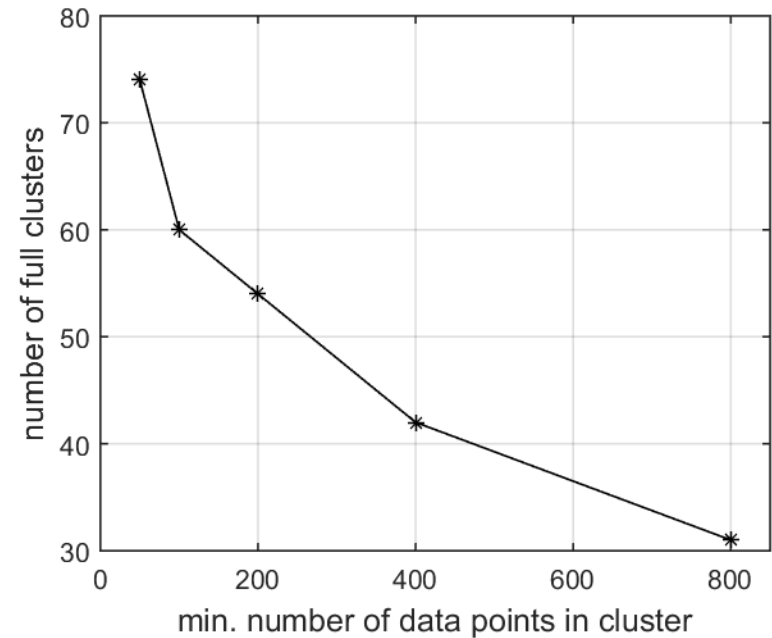
- Confidence interval and standard deviation normed by mean value
- Averaged analysis figures of full clusters

# Analysis – Minimum Number of Data Points

confidence interval



number of full clusters



Normed standard deviation is approximately constant!

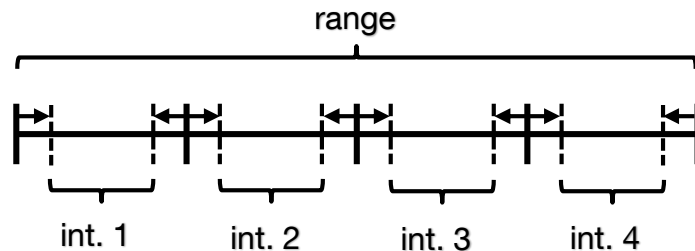
**For further analyses: min. number of data points = 2 x number of flights**



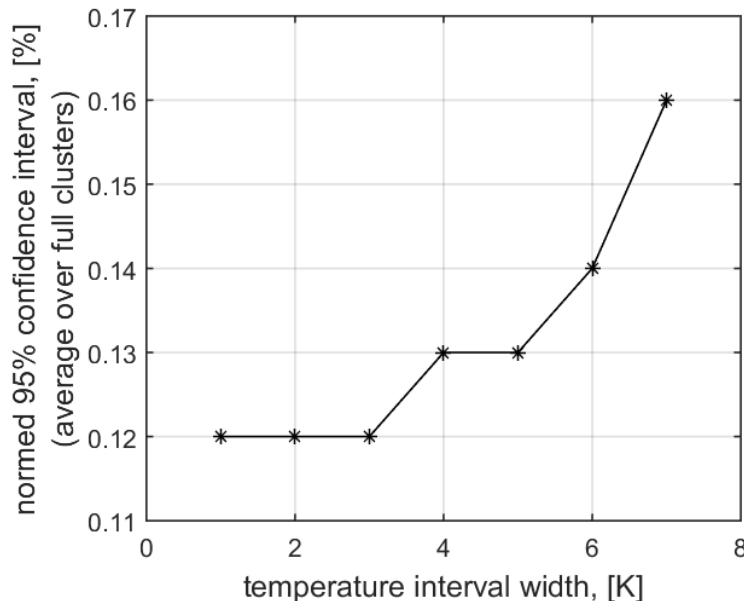
# Analysis – Interval Width

## Variation of temperature interval width

➤ From 7K to 1K

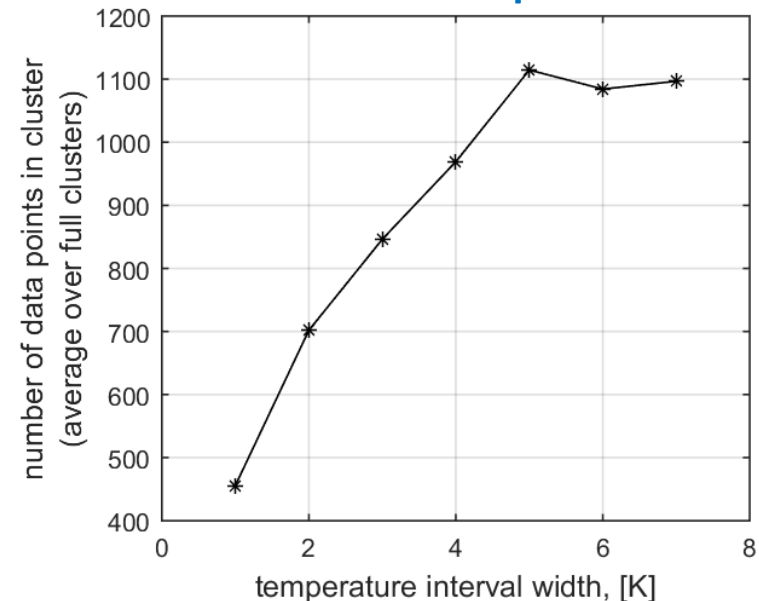


### confidence interval



Contributing Factor	Unit	Width of Interval
Pressure Altitude	[m]	50
Fan Speed	[-]	0.006
Mach Number	[-]	0.006
Temperature	[K]	7 → 1

### number of data points

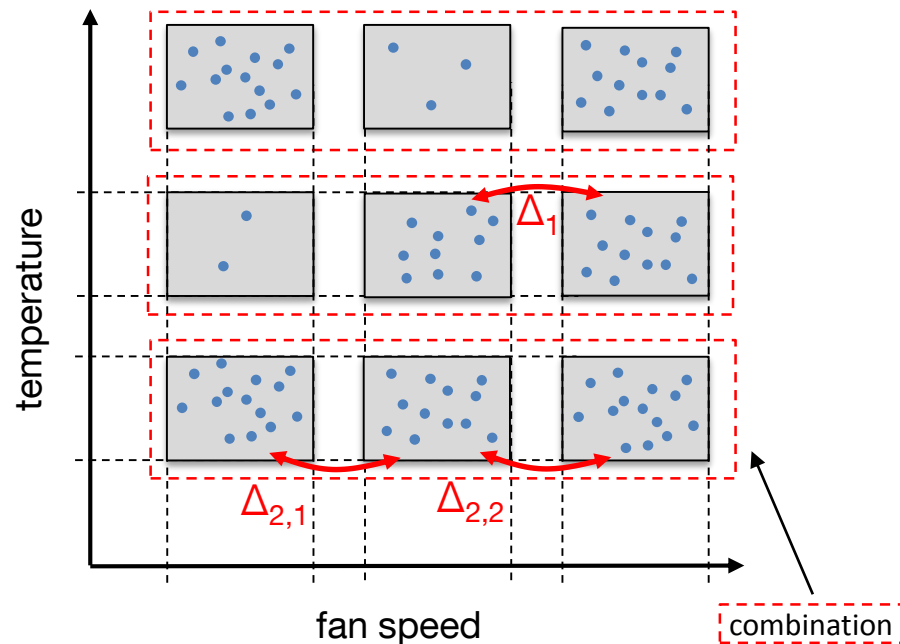


# Analysis – Sensitivity Analysis

## How well do influencing factors separate the fuel flow?

### Separation of adjacent full clusters

- Difference of mean values  $\Delta_i$  of fuel flow distributions in full clusters
- Only difference in direction of one influencing factor
  - Separation for all combinations of remaining influencing factors
  - Only combinations considered, where adjacent full clusters exist
  - Example: 3 “combinations” of temperature



### Mean value of $\Delta_{i,k}$ for one combination of remaining influencing factors

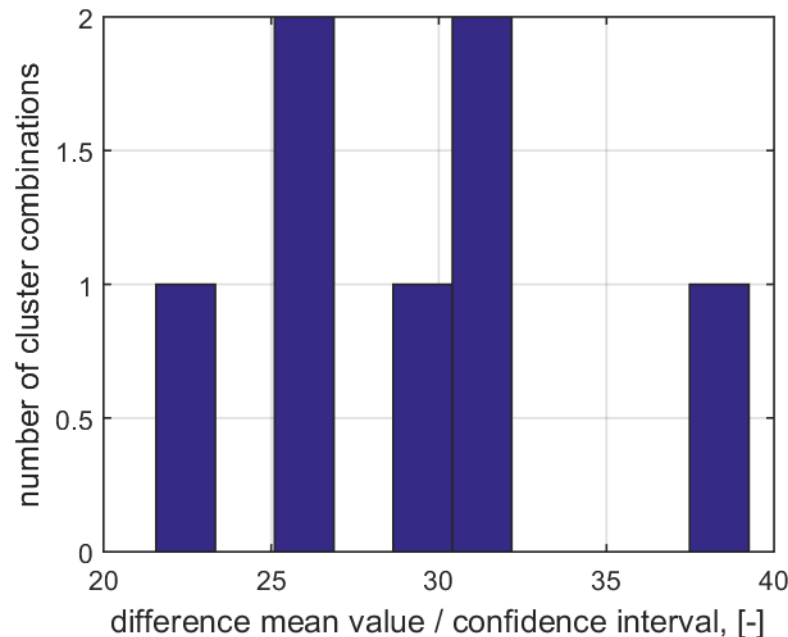


$$\Delta_i = \text{mean}(\Delta_{i,1}, \Delta_{i,2}, \dots, \Delta_{i,k})$$

# Analysis – Sensitivity Analysis

## Example: separation through fan speed

- decreased intervals of influencing factors
- $\Delta$ 's normed by confidence interval widths



7 combinations with adjacent full clusters

Fan speed leads to best separation

Separated by 22-39 confidence intervals

Separation increases for smaller intervals of influencing factors

- Clustering by temperature also delivers wide separation

- Number of influencing factors has no great influence

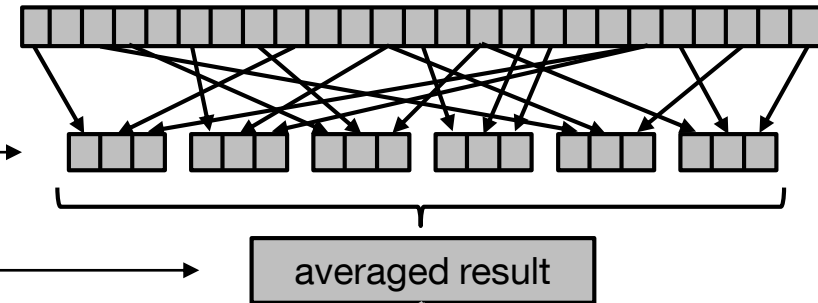
# Analysis – Number of Flights

## Data base:

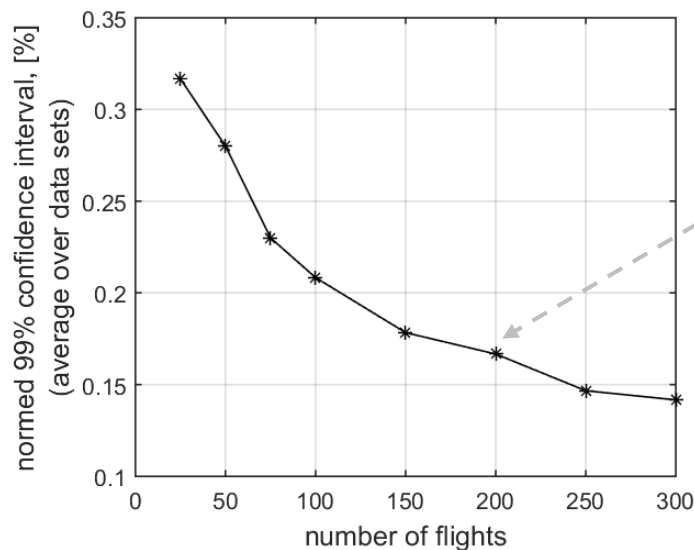
- 352 Flights of one aircraft

## Method:

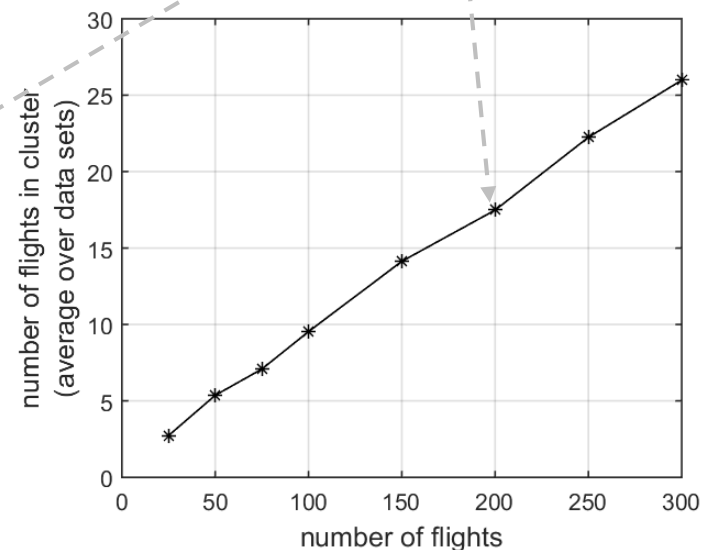
- For each number of flights, random pick of 6 data sets of flights
- Average over results of the 6 random sets



## confidence interval



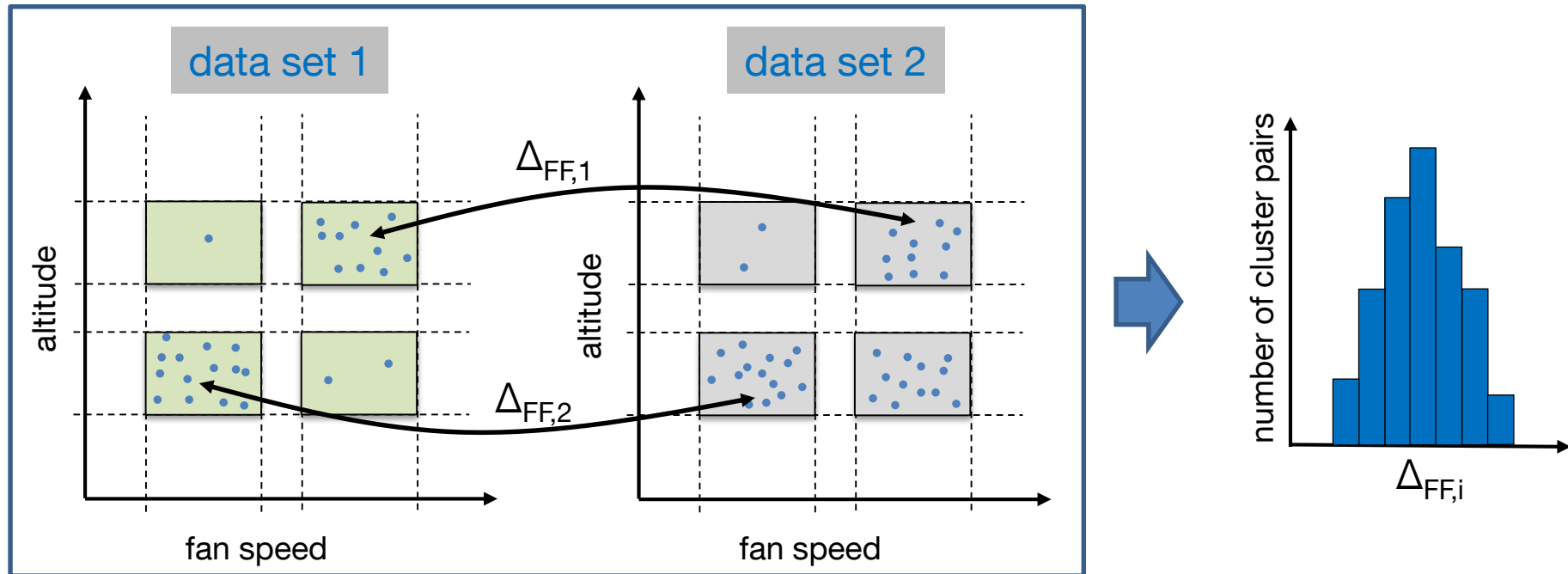
## number of flights in cluster



# Concept of Clustering – Comparing Data Sets (Reminder)

Compare pairs of full clusters of two different data sets

- Calculate difference of mean values of both full clusters ( $\Delta_{FF,i}$ )



Comparison of multiple data sets via: Mean values of  $\Delta_{FF}$ -distributions of each pairwise combination of data sets

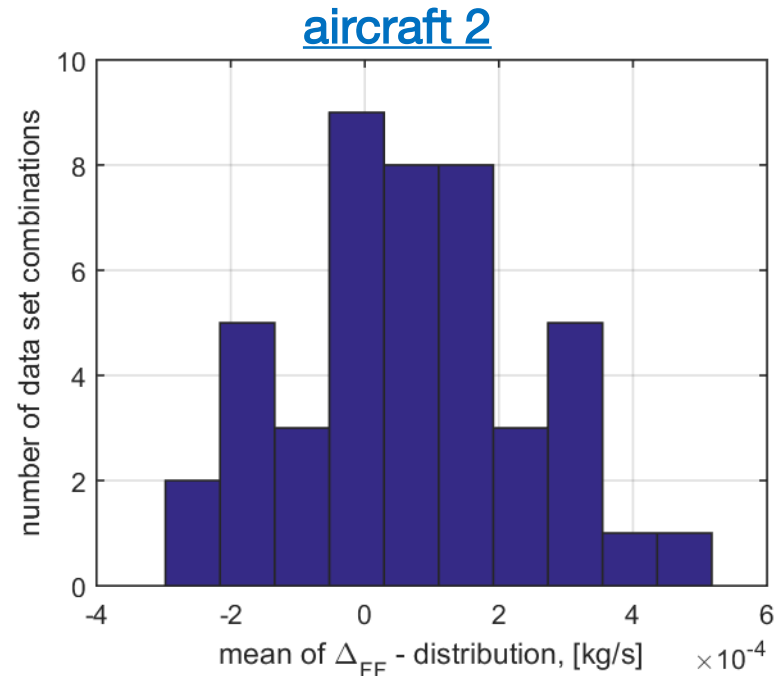
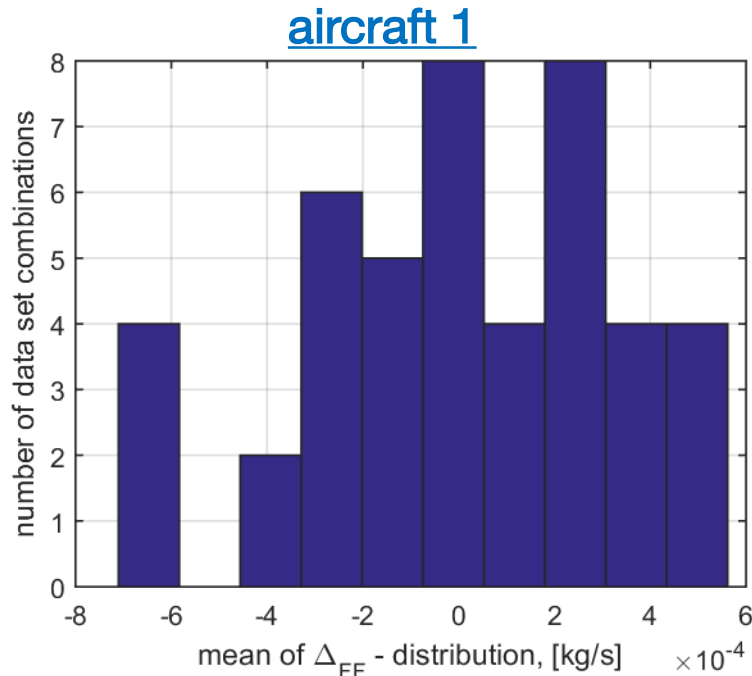
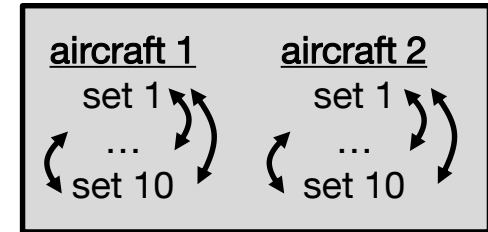
# Comparison of two Sets of Flights

## Data Base:

- Two aircraft of same type, data from June and July 2014
- 10 random data sets of 100 flights for each aircraft

## Method (part 1):

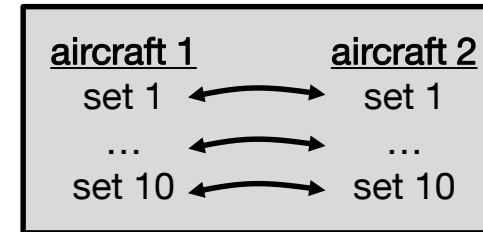
- Compare 10 data sets of one aircraft amongst each other
- Mean value of  $\Delta$ -distribution for every combination of two data sets (10 sets  $\rightarrow$  45 combinations)



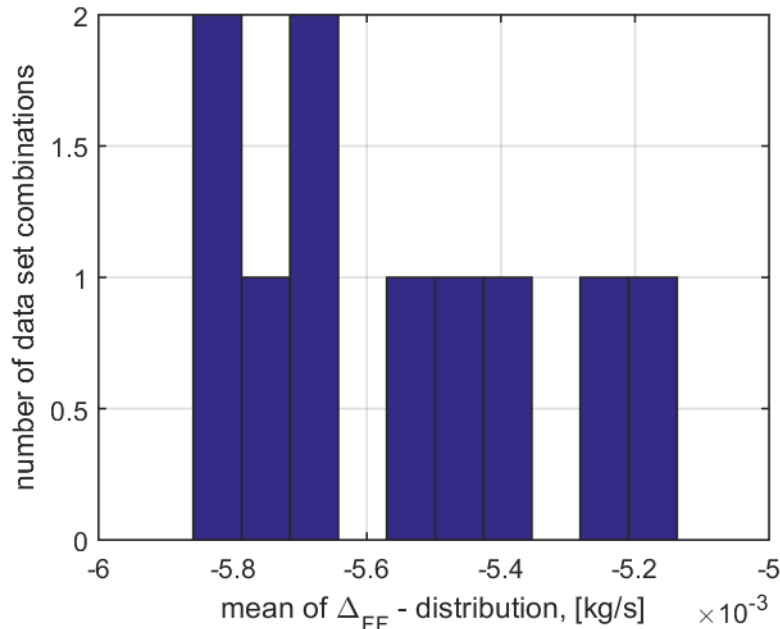
# Comparison of two Sets of Flights

## Method (part 2):

- Mean value of  $\Delta$ -distribution between sets 1-10 of both aircraft



## both aircraft compared



**significant difference evident**

## Value range for each aircraft:

- Aircraft 1:  $(-8) - (+6) \times 10^{-4}$  kg/s
- Aircraft 2:  $(-4) - (+6) \times 10^{-4}$  kg/s

## Value range for comparison:

- $(-6) - (-5) \times 10^{-3}$  kg/s
- About 1% difference between aircraft

# Summary / Conclusion

- Significant difference for two aircraft found with only four influencing factors
- Clusters best separated by fan speed
- Saturation for confidence intervals for increasing number of flights/data points
- Smaller intervals for fan speed and temperature lead to smaller confidence intervals



Source: AirBaltic



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The AirBaltic logo, featuring the word "airBaltic" in a bold, dark blue sans-serif font. The "air" is in lowercase and "Baltic" is in uppercase. The logo is set against a bright yellow rectangular background.

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**Thank you for your attention**